

Bus 274: Further Statistics for Business

Spring 2010

PROBLEM SHEET # 4

Problem 1: Suppose in a sample of 25 people, the sample mean height was observed to be 70 inches. Suppose also that height is normally distributed with a known standard deviation of $\sigma = 3$.

- Give an example of an industry which will be interested in body heights of people.
- Construct a 95% confidence interval for μ .
- Would you reject the hypothesis $H_0 : \mu = 71$ versus $H_1 : \mu \neq 71$ on the basis of the observations, when testing at level $\alpha = 0.05$?
- Explain in a few words what the terms “type I error” and “type II error” mean in the test problem in (c). Considering the outcome of the test in (c), could we have made a type I or type II error?
- Now assume the population variance is not known, and 3 is the standard deviation of the sample (that is, $s = 3$). Which test statistic for the test in (c) would you be using in this case?
- Would you expect the power of the test to increase or to decreased as we change the statement from “*The true mean equals 72*” to “*The true mean equals 78*”?

Problem 2: A manufacturer of tires wants to make sure the tires last on the average at least 22000 miles. Suppose a random sample of five tires had a sample mean of $\bar{x} = 22819$ and a sample standard deviation of $s = \hat{\sigma} = 1295$ miles. We assume that the “life” of a tire, in terms of miles, is normally distributed.

- Which null hypothesis H_0 has to be tested against which alternative H_1 ? Why?
- Carry out the test. Use a significance level of $\alpha = 5\%$.
- Briefly explain in words what we can conclude about the quality of the tires in view of the result in (b).

Problem 3: The average daily return (observations from one year, 250 values) on a stock index was 0.3%, and the standard deviation of the daily returns was 2.6%.

- Test the null hypothesis that the expected daily return is 0%. (Use a 5% level of significance.)
- Compute the probability that the average daily return for 250 days takes on a value outside the interval $[-0.3\%, +0.3\%]$ under the assumption that the hypothesis under (a) is true. (This is the p -value of the null hypothesis in (a).)