

## Bus 273: Statistical Analysis for Business

Fall 2014

### PROBLEM SHEET # 10

**Problem 1:** Severe earthquakes occur according to a Poisson process with intensity  $\lambda = 0.2/\text{year}$  in a certain geographical region.

- a) What is the expected time between two successive severe earthquakes?
- b) Compute the probability that there will be no severe earthquake during the next 10 years.

**Problem 2:** One of the items used in a car repair shop (araba tamircisi) is a certain type of windshield (ön cam). The repair shop needs an average of 2 units of this windshield per month. We assume that demand in different months is independent.

- a) Why is it reasonable to consider  $N = \text{monthly demand of this windshield}$  a random variable?
- b) Explain why we can assume that  $N \sim \text{Po}(\lambda)$ . — What is the value of  $\lambda$  in this case?
- c) Write the expression, with the correct parameter, for the probability that no unit will be needed during a month, that is:  $P(N = 0)$ .
- d) Write the expression, with the correct parameter, for the probability that more than three units will be needed during a month, that is:  $P(N > 3)$ .
- e) Let  $X = \text{length of the time interval (in days) between two successive requirements of the windshield}$ . Find the distribution of  $X$ .
- f) Let  $M = \text{required number of units of the windshield in a year}$ . Find the expectation and the variance of  $M$ .
- g) Demand for the windshield was above average in December. What does this mean for demand in January? Discuss briefly.
- h) Why is it useful to analyze windshield demand in car repair shops? Discuss briefly.